

# Math 534A Homework 8.

Due 11/18

1. Let  $\text{SL}(n, \mathbb{R})$  be the set of  $n \times n$  matrices with determinant equal to 1. Prove that  $\text{SL}(2, \mathbb{R})$  is a manifold of dimension  $n^2 - 1$ . Hint: you may use the fact that if you have a matrix smooth function  $M(t)$  and  $\det M(t) > 0$  then  $\frac{d}{dt} \log \det M(t) = \text{tr} \left( M^{-1} \frac{dM}{dt} \right)$  (why is this true?).
2. \*Lee 11-1
3. Lee 11-4.
4. Lee 11-7.

Note: \* means that I want someone to look at your answer and attest to it before submitting.