

**MATH 464**  
**HOMEWORK 1**

SPRING 2016

The following assignment is to be turned in on  
**Thursday, January 28th, 2016.**

1. Let  $A$ ,  $B$ , and  $C$  be events (subsets) of a sample space  $\Omega$ .  
Write each of the following events in terms of  $A$ ,  $B$ , and  $C$  using intersections, unions, and complements.

- (a) None of  $A$ ,  $B$ ,  $C$  occurs.
- (b) At least two of  $A$ ,  $B$ ,  $C$  occur.
- (c) Exactly one of  $A$ ,  $B$ ,  $C$  occurs.
- (d) Exactly two of  $A$ ,  $B$ ,  $C$  occur.
- (e) Exactly three of  $A$ ,  $B$ ,  $C$  occur.

**Hint:** Read Section 1.2 of the book or the pdf file on semantics.

2. Do exercises 10, 12, and 17 on pages 5 and 7 of the book.

3. Consider an *unfair* coin which has probability  $1/3$  for heads and  $2/3$  for tails. Do an experiment where you flip this coin until you get heads and stop.

- (a) Describe the sample space.
- (b) What is the probability it takes exactly 5 flips?
- (c) What is the probability it takes at least 3 flips?