DENISE AND CHAD

Use the following background information and definitions to answer the questions below.

- * A person "likes" another person if they have a positive affection for them.
- * A person is happy when he or she is" liked" by someone else. A person is unhappy if they he or she is disliked by someone.
- * A couple is "happy" when they both like each other. A couple is unhappy when they both dislike each other.
- * Denise and Chad meet at time t = 0 where t is measured in weeks.
- * Denise's affection for Chad is characterized by $\sin\left(\frac{9\pi t}{10}\right)$ for $0 \le t \le a$ for some constant *a*. Otherwise her affection has the value of zero.
- * Chad's affection for Denise is characterized by $2\sin\left(\frac{7\pi t}{10}\right)$ for $0 \le t \le a$ for some constant *a*. Otherwise his affection has the value of -2.
- 1. Who has the greater emotional range? What is that range?
- 2. Whose emotions fluctuate most rapidly? What is that fluctuation?
- 3. When did Denise and Chad have no feelings for each other, but their affections were increasing?
- 4. When did Denise like Chad intensely, but Chad disliked Denise intensely?
- 5. When was Denise a "happy" individual?
- 6. When were Denise and Chad "happy" as a couple?
- 7. Find the value of *a* and describe their relationship for t > a.
- 8. During the time $0 \le t \le a$, what percent of the time were Denise and Chad "happy" as a couple?