## Approximating definite integrals:

1. The characteristic of $f(x)$ is given in the first column. For each rule, determine if the rule will produce an overestimate or underestimate of a definite integral.

| $f(x)$ | Left hand | Right Hand | Mid point | Trapezoid |
| :--- | :--- | :--- | :--- | :--- |
| Increasing and <br> Concave up |  |  |  |  |
| Decreasing and <br> Concave up |  |  |  |  |
| Increasing and <br> Concave down |  |  |  |  |
| Decreasing and <br> Concave down |  |  |  |  |

2. Estimate the value of $\int_{0}^{4} e^{x^{2}} d x$ with $n=4$, for each of the given rules. Complete the table with exact values (do not use calculator program). Illustrate each rule in the space provided below.
a. Left Hand Rule

| $x$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $e^{x^{2}}$ |  |  |  |  |  |

$$
\operatorname{Left}(4)=
$$

b. Right Hand Rule

| $x$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $e^{x^{2}}$ |  |  |  |  |  |

$$
\operatorname{Right}(4)=
$$

c. Midpoint Rule

| $x$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $e^{x^{2}}$ |  |  |  |  |  |

$$
\operatorname{Mid}(4)=
$$


d. Trapezoid Rule

| $x$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $e^{x^{2}}$ |  |  |  |  |  |

