

- (c) What is the probability that the average weight of four randomly selected monkeys is between 12 and 16 pounds?

$$\begin{aligned}P(12 \leq \bar{x} \leq 16) &= P\left(\frac{12-15}{1.5} \leq Z \leq \frac{16-15}{1.5}\right) \\&= P(-2.0 \leq Z \leq 0.67) \\&= 0.7486 - 0.0228 \\&= 0.7258\end{aligned}$$

- (d) How many weights must be averaged in order to obtain a standard deviation of one pound?

$$n = \left(\frac{3}{1}\right)^2 = 9$$

Nine weights must be averaged in order to obtain a standard deviation of one pound.

3. Forty percent of Americans have type A blood.

- (a) Find the mean and standard deviation of the sampling distribution of the proportion of 500 randomly selected Americans that have type A blood?

$$\mu_{\hat{p}} = 0.40$$

$$\sigma_{\hat{p}} = \sqrt{\frac{0.40(1-0.40)}{500}} \approx 0.0219$$

- (b) Find the probability that the proportion of 500 randomly selected Americans that have type A blood is greater than 0.45.

$$\begin{aligned}P(\hat{p} > 0.45) &= P\left(Z > \frac{0.45-0.40}{0.0219}\right) \\&= P(Z > 2.28) \\&= 1 - P(Z \leq 2.28) \\&= 1 - 0.9887 \\&= 0.0113\end{aligned}$$

- (c) Explain why the computations used in (b) are justified.

The computations in (b) are justified because $np = 500(0.40) = 200 \geq 10$, $n(1-p) = 500(1-0.40) = 300 \geq 10$, and the population of Americans is greater than or equal to $500 * 10 = 5000$.

- (d) Without making any computations, explain how the standard deviation of the sampling distribution of the proportion of 250 randomly selected Americans that have type A blood would compare to the standard deviation computed in (a).

The standard deviation of the sampling distribution of the proportion of 250 randomly selected Americans that have type A blood would be larger than the standard deviation computed in (a).