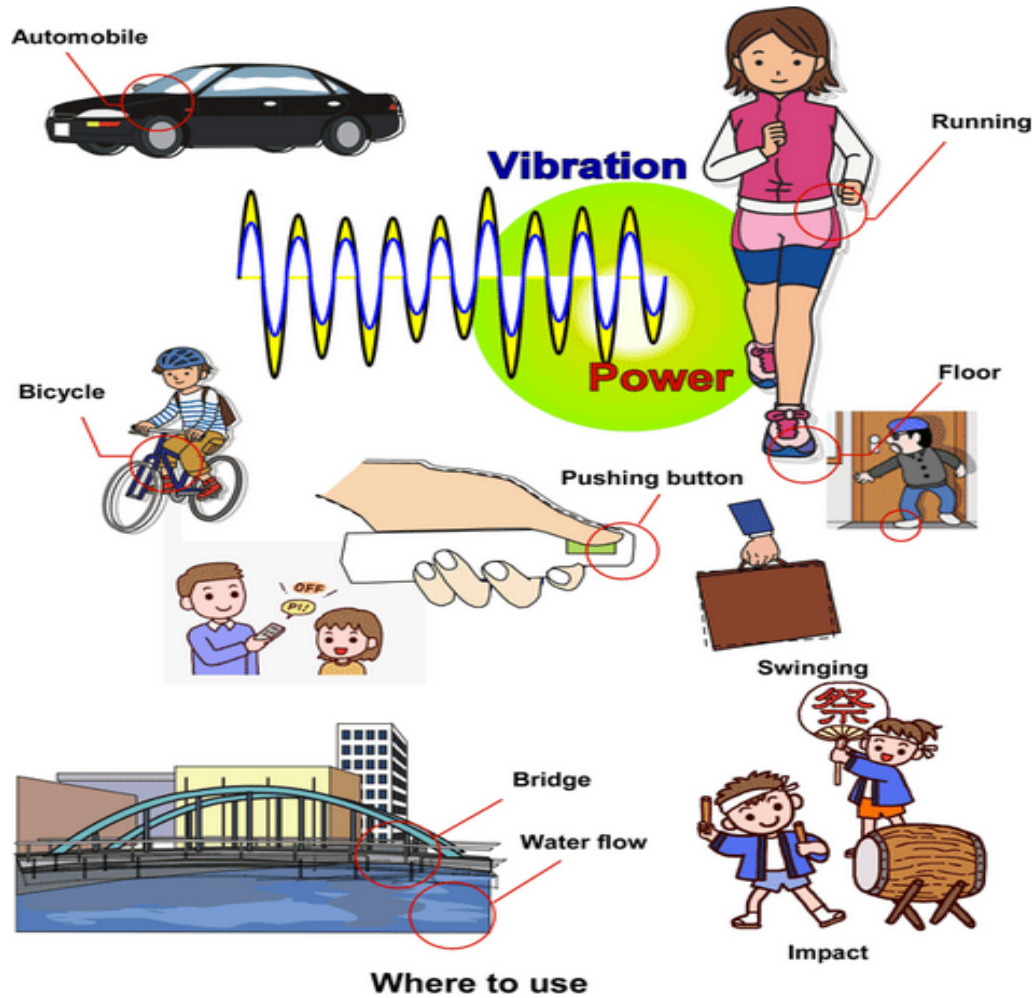


Nonlinear Energy Harvesting

Brent Cook; Luis Sanchez; Larissa Szwez; Joseph Tang;
Yuhao Pan; Joshua Paul

Introduction

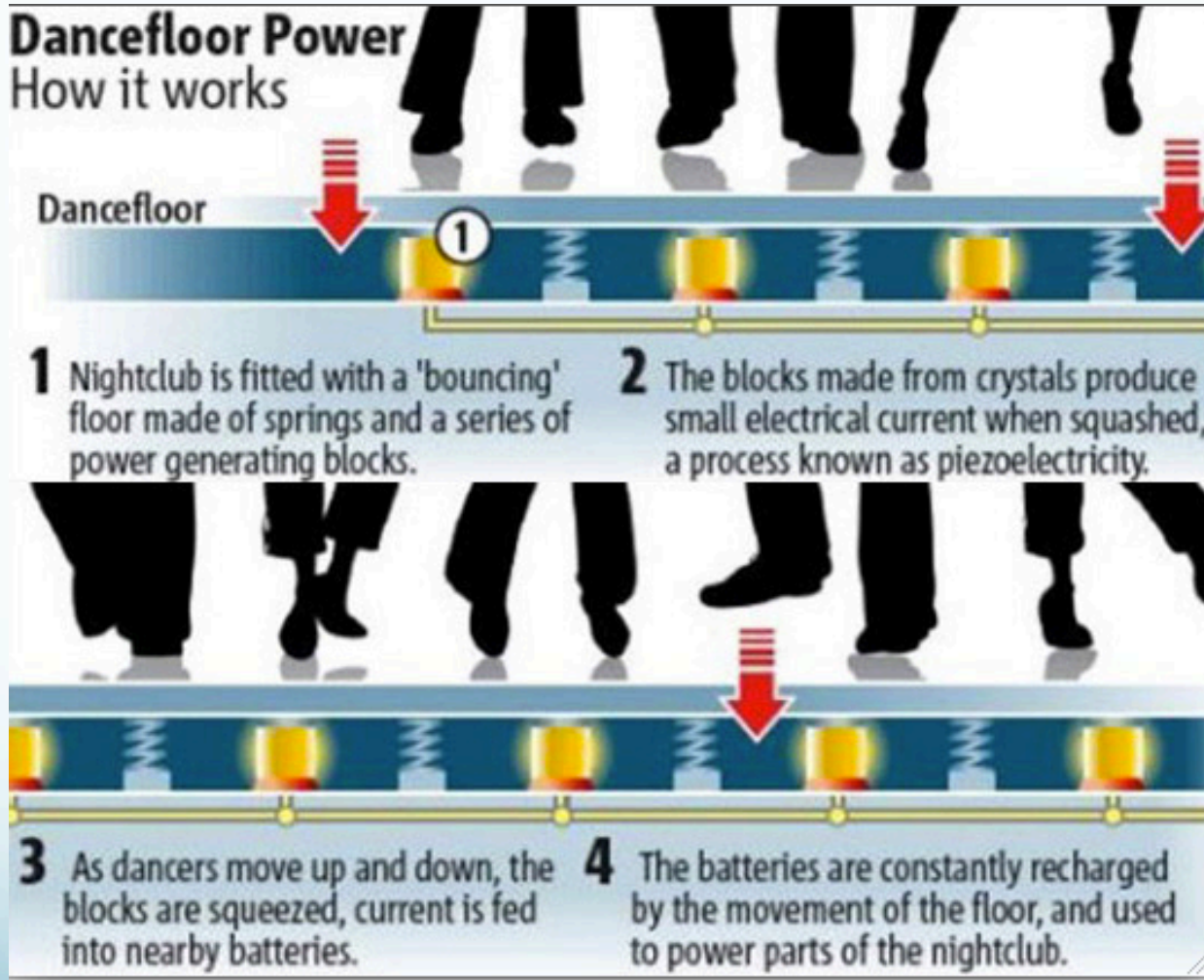
Vibration → → Energy



Energy Harvesting

- **Ambient Energy Harvesting becoming popular in research to charge mobile devices such as cell phones**
- **Multiple ways to harvest energy (convert kinetic energy to electrical energy)**
 - **Capacitive**
 - **Inductive**
 - **Piezoelectric**

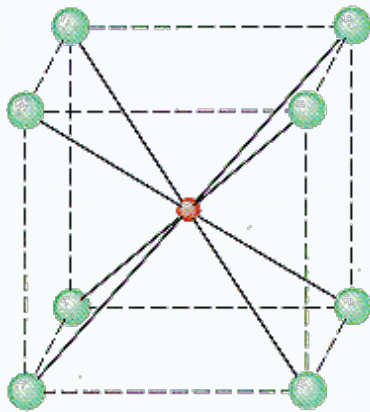
Application



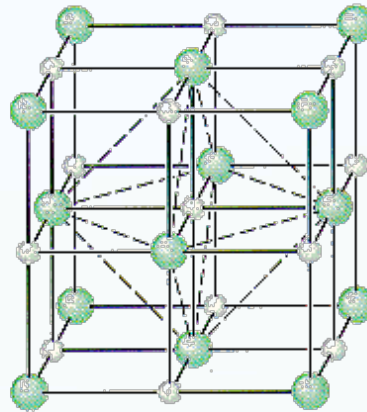
What is piezoelectricity?



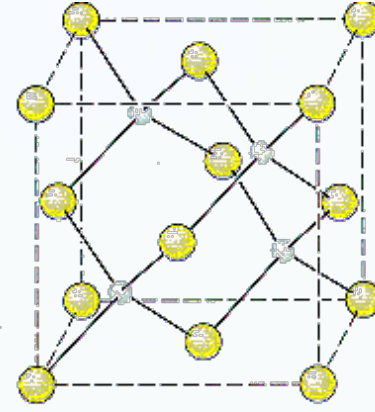
Crystal Structures



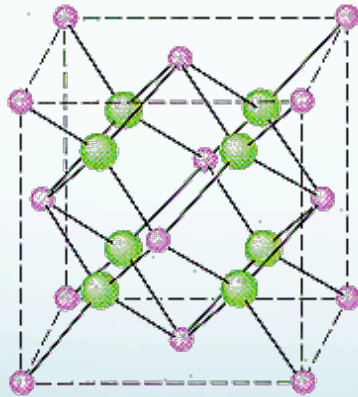
CsCl



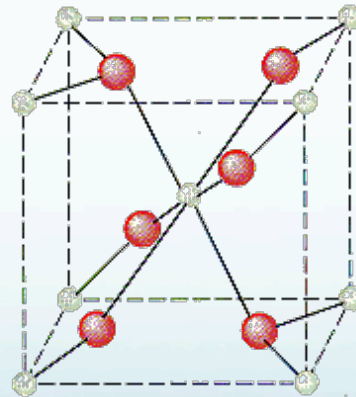
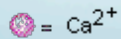
NaCl



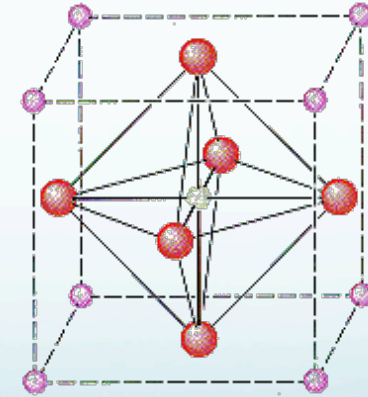
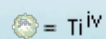
Zinc blende (cubic ZnS)



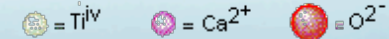
Fluorite (CaF₂)



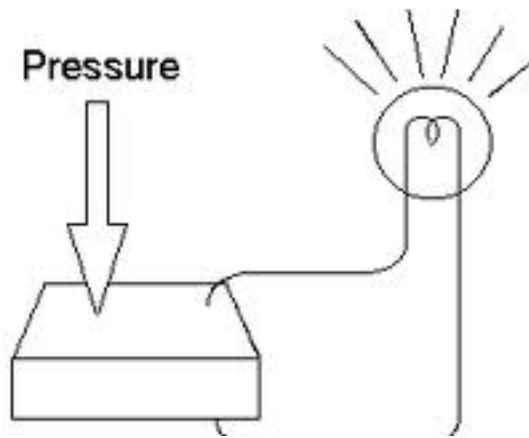
Rutile (TiO₂)



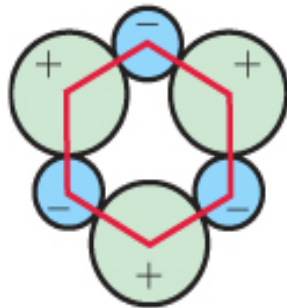
Perovskite (CaTiO₃)



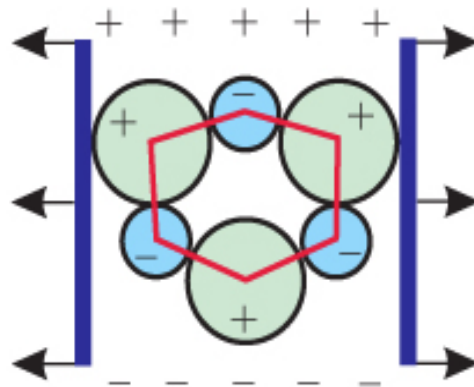
Piezoelectric Effect



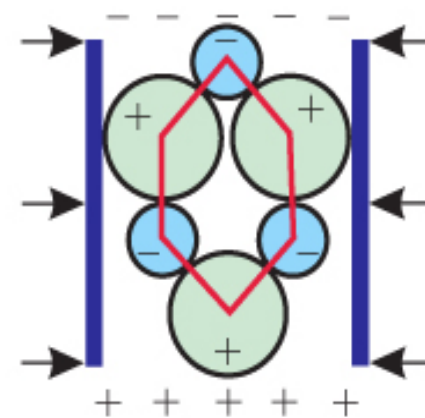
No Stress



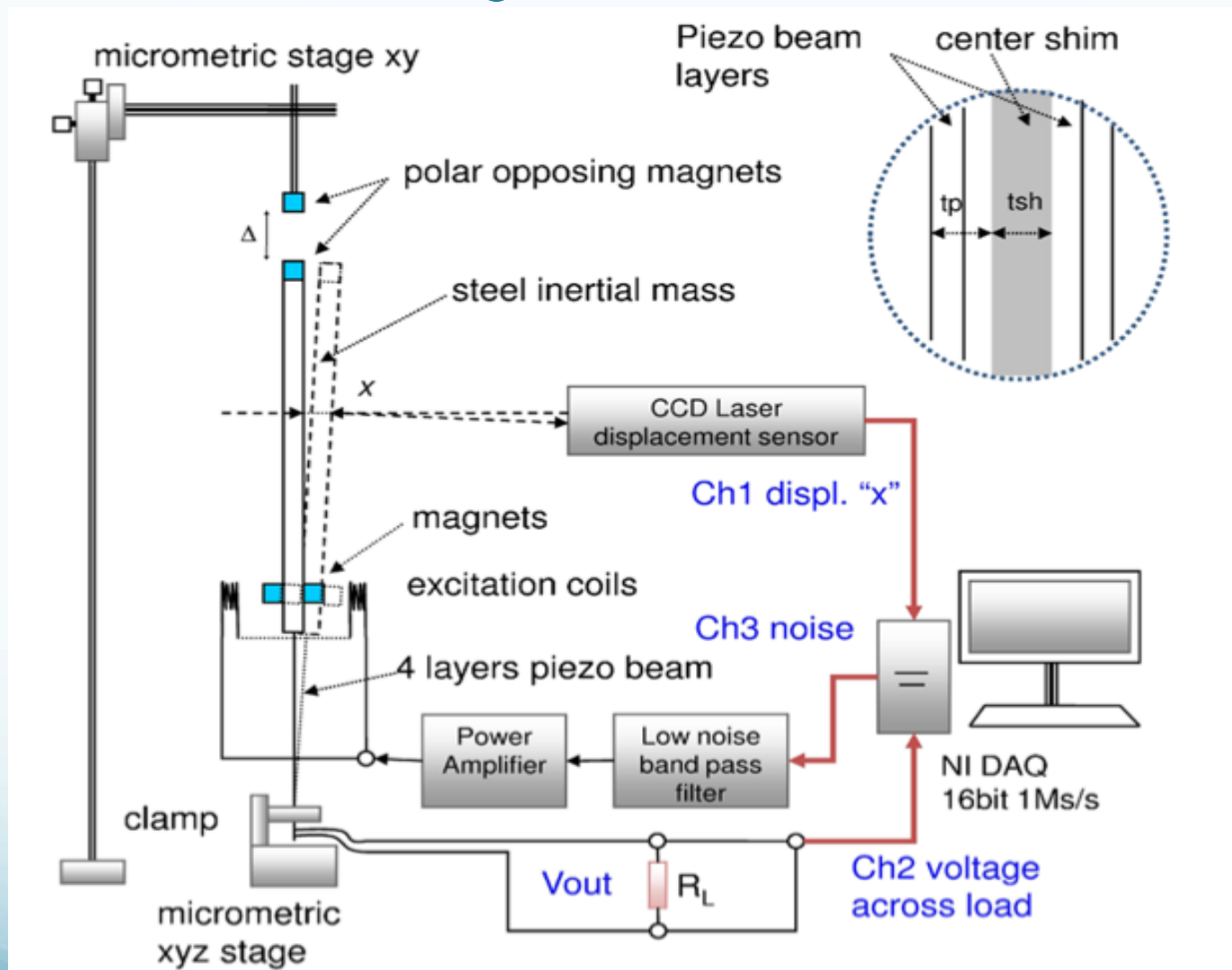
T
Tension



C
Compression



Physical Model



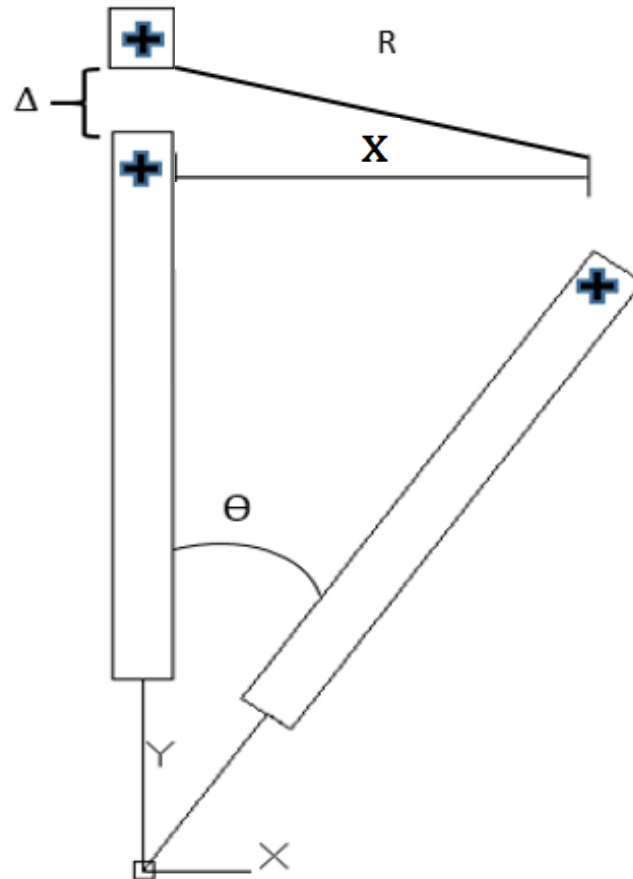
Equation of Motion

$$m_{eff}\ddot{x} = \frac{dU(x)}{dx} - \gamma\dot{x} - K_v V(t) + \sigma\varepsilon(t)$$

| Equation | Meaning |
|------------------------|--|
| $m_{eff}\ddot{x}$ | The kinetic force of the oscillator |
| $U(x)$ | The potential energy function of the oscillator |
| $\gamma\dot{x}$ | Energy dissipation due to bending of the piezoelectric |
| $K_v V(t)$ | Energy transferred to the resistor |
| $\sigma\varepsilon(t)$ | Vibrational force that drives the oscillations; a stochastic process |

Source: Cottone, F; Vocca, H; Gammaitoni, L; Phys. Rev. Lett. **102** 080601 (2009)

Physical Model



Deriving Equation

Assume $\theta \ll 1$

$$F_{\text{res}} = -K_B \cdot d \rightarrow \int F_{\text{res}} = \int -K_B \cdot d \rightarrow U_{\text{res}} = \frac{1}{2} d^2 + C_1$$

$$F_m = \frac{\alpha}{R^4} \rightarrow \int F_m = \int \frac{\alpha}{R^4} \rightarrow U_m = \frac{\alpha}{-3R^3} + C_2$$
$$\Rightarrow U_m = -\frac{\alpha}{3(x^2 + \Delta^2)^{\frac{3}{2}}} + C_2$$

Analyzing

$$U(x) = Kx^2 + (ax^2 + b\Delta^2)^{-3/2} + c\Delta^2$$

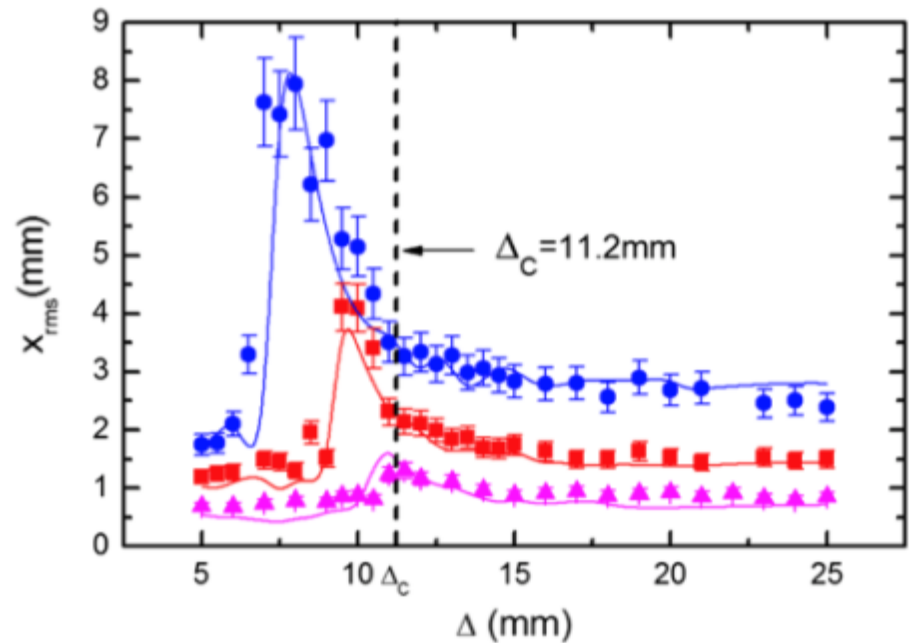
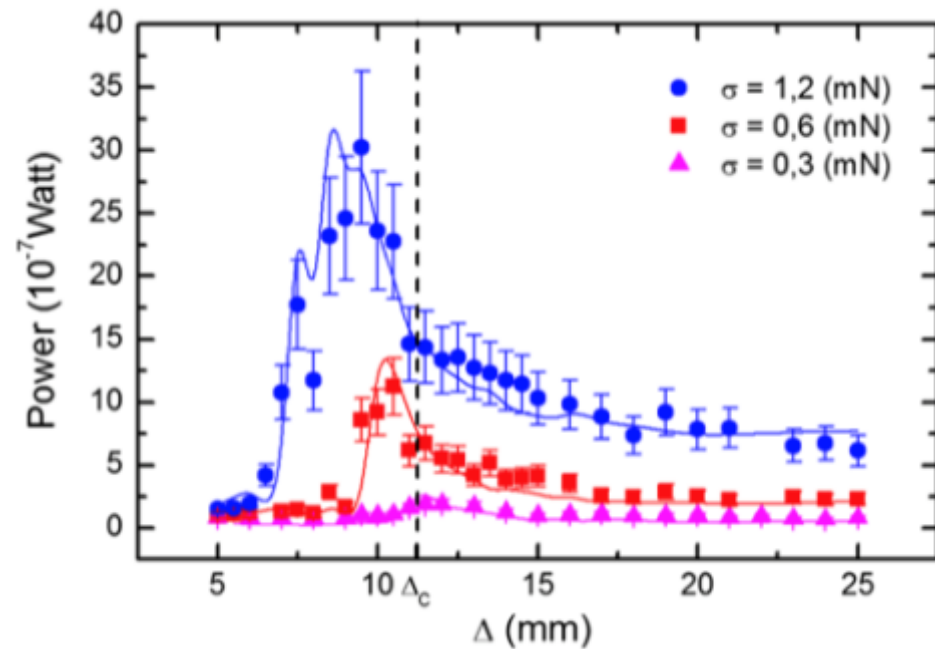
$$U(x) = \frac{K_{eff}}{2}x^2 + \left(d^2 \left(\frac{\mu_0 M^2}{2\pi d}\right)^{-\frac{2}{3}} * x^2 + \left(\frac{\mu_0 M^2}{2\pi d}\right)^{-\frac{2}{3}} * \Delta^2\right)^{-3/2} + \frac{K_{eff}}{2d^2}\Delta^2$$

| Equation | Meaning |
|-----------|---|
| K_{eff} | Effective elastic constant of the pendulum |
| μ_0 | The permeability constant |
| M | Effective magnetic moment of both magnets |
| d | Geometrical parameter related to the distance between the measurement point and the pendulum length |
| C | Capacitance of the piezoelectric |
| R_L | Resistive load in the circuit |
| K_c | Coupling constant of the piezoelectric material |

$$\dot{V}(t) = K_c \dot{x} - \frac{V(t)}{R_L C}$$

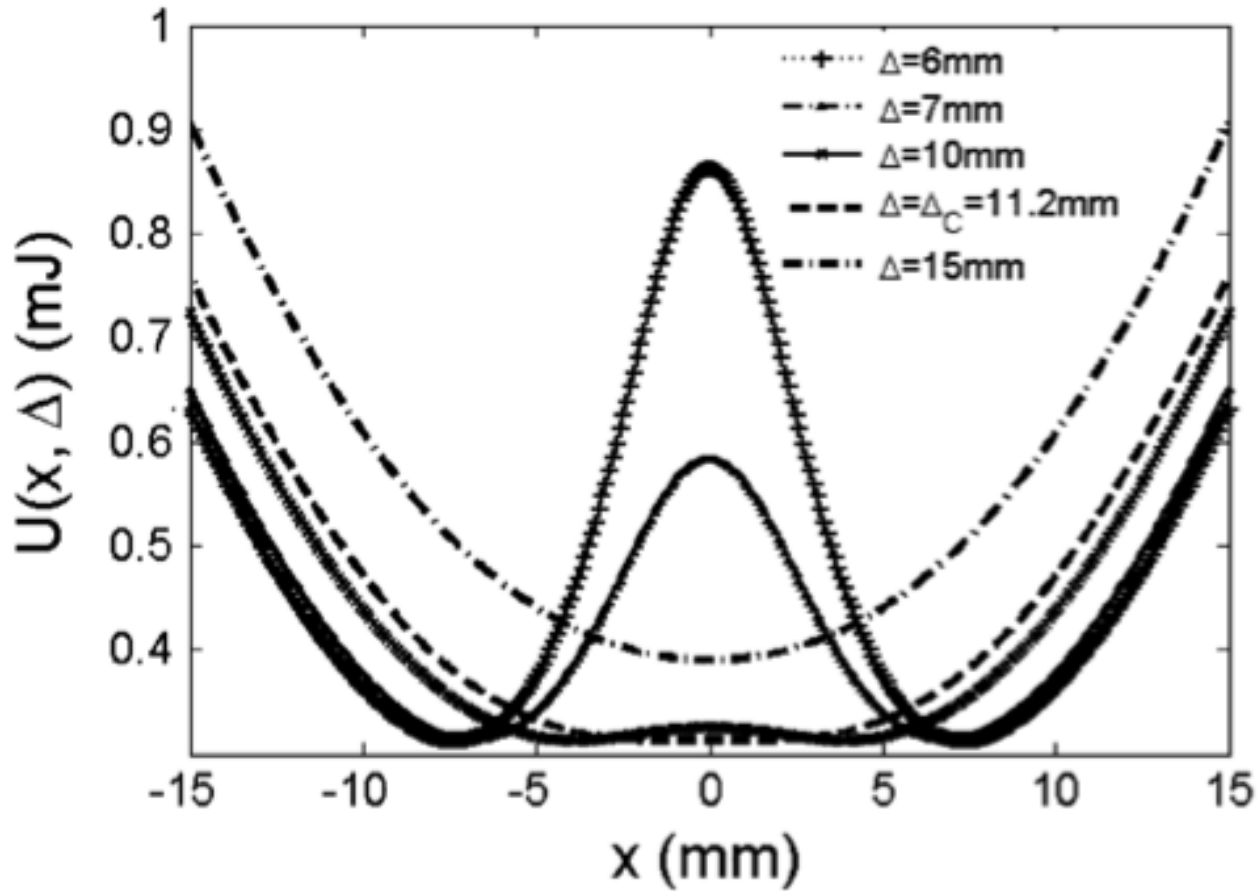
Source: Cottone, F; Vocca, H; Gammaitoni, L; Phys. Rev. Lett. **102** 080601 (2009)

Results



Source: Cottone, F; Vocca, H; Gammaitoni, L; Phys. Rev. Lett. **102** 080601 (2009)

Results



Source: Cottone, F; Vocca, H; Gammaitoni, L; Phys. Rev. Lett. **102** 080601 (2009)

Our Problem



Future Plan

General Idea:

- **Determine how different positions of pendulum at varying initial angles affect energy output**
- **Create probability distribution of different phone orientations throughout the day**
- **Analyze gravity on pendulum in various positions and how this affects voltage generation**

Questions?

Thank you!