

Only the answers to even numbers are given.

1. Chapter Review Chapter 2:

36) a) IV b) III c) II d) I e) IV f) II

2. Chapter Review Chapter 3:

22) $\frac{dy}{dx} = 2e^{2x} \sin(3x) (\sin(3x) + \cos(3x))$

34) $H(t) = (-cat^2 + 2at - bc) e^{-ct}$

60) a) 1 b) 2 c) 3 d) 3 e) $-5/16$ f) 13

62) a) 20 b) $11/9$ c) -4 d) -24 e) $\sin 3 - 8 \cos 3$ f) $4 \ln 3 - 16/3$

80) Draw a picture of a right triangle with height 2, other leg x , and hypotenuse s . We then can use the Pythagorean theorem to get $x = \sqrt{s^2 - 4}$. We find that $\frac{dx}{dt} = \frac{s}{x} \frac{ds}{dt} = 233.2$ mi/hr.

82) a) We see that $V = \frac{k}{P}$ so volume decreases. b) Since $PV = k$ and $P = 2$ when $V = 10$ we get $k = 20$. Thus using the chain rule we eventually get

$$\frac{dV}{dt} = -\frac{20}{P^2} \frac{dP}{dt}$$

and then we get $\frac{dV}{dt} = -0.25$ cm³/min.

3. Check your understanding Chapter 2:

10) False. If f' is positive then f is increasing. f' could be negative and increasing and then f is decreasing.

12) True. If $f(x) = mx + b$ then $f'(x) = m$, constant.

22) True. For example, $f(x) = x$ is differentiable at every point and also continuous.

4. Check your understanding Chapter 3:

2) False. $\frac{d}{dx}(\pi/x^2) = -2\pi/x^3$

6) True. The slope is the derivative and the derivative of $f + g$ is $f' + g'$.

5. I leave it to you to plug in the values, but I'll take the derivatives for you:

a) $3f'(12)$, b) $f'(4) + 9g'(4)$, c) $f'(f(4)) \cdot f'(4)$, d) $2f(4)f'(4)$, e) $f'(4)g(4) + f(4)g'(4)$, f) $\frac{g(4)f'(4) - f(4)g'(4)}{g(4)^2}$, g) $f'(g(4))g'(4)$, h) $g'(f(4))f'(4)$, i) $g'(f(f(4))) \cdot f'(f(4)) \cdot f'(4)$, j) $(\cos g(4))g'(4)$, k) $3f(4)^2 f'(4) - 2(4)f'(16)$, l) $3f'(12)\sqrt{4} + f(12)\frac{1}{2\sqrt{4}}$

6.a) 1st derivative = $2x \sin x + x^2 \cos x$, 2nd derivative = $2 \sin x + 2x \cos x + 2x \cos x - x^2 \sin x = 2 \sin x + 4x \cos x - x^2 \sin x$

b) 1st derivative = $4(x+1)^3 \sqrt{x} + \frac{1}{2}(x+1)^4 x^{-1/2}$, 2nd derivative = $12(x+1)^2 \sqrt{x} + 2(x+1)^3 x^{-1/2} + 2(x+1)^3 x^{-1/2} - \frac{1}{4}(x+1)^4 x^{-3/2} = 12(x+1)^2 \sqrt{x} + 4(x+1)^3 x^{-1/2} - \frac{1}{4}(x+1)^4 x^{-3/2}$

7. State the definitions of derivative of f at 4 and of the statement “ f is continuous at 4.”

$$f'(4) = \lim_{h \rightarrow 0} \frac{f(4+h) - f(4)}{h}.$$

f is continuous at 4 if

$$\lim_{x \rightarrow 4} f(x) = f(4).$$

8.

a) $3x^{300} + 300(3x+2)x^{299} = 903x^{300} + 600x^{299}$, b) $\frac{6x^2+2x^3-1}{(x+2)^2}$ c) $\frac{1}{3}(2x+2)(x^2-2x)^{-2/3}$, d) $\frac{(2x^2-1)e^x - 2xe^x}{2x^2-1}$, e) $\sin(-x)$, f) $3999(2x+3)^{1998}$, g) $\frac{99}{100}(x+3x^3)^{98}(1+9x^2)$, h) $5e^{5x+1}$, i) $2 \sin x \cos x$, j) $2x(\ln 2)2^{x^2+1}$, k) $2xe^x \sin x + x^2e^x \sin x + x^2e^x \cos x$, l) $-\frac{1}{2\sqrt{x}} \sin \sqrt{x}$, m) $\frac{\sin x - x \cos x}{\sin^2 x}$, n) 0, o) $-\frac{e^{x^2} - 2x^2e^{x^2}}{e^{2x^2}}$, p) ex^{e-1} , q) $(\ln 10)10^{\sin(x^3+2)} \cos(x^3+2)3x^2$

9. a) $p(x) = \frac{7}{2}x^2 + 3x + 2$. b) $E(x) = 2(4^x)$ Give an exponential function $E(x)$ which satisfies $E(0) = 2$, $E'(0) = 2 \ln 4$.

10. Give the equation of a tangent line to the following curves at $x = 1$.

a) $y = 8x - 4$ b) $y = \frac{1}{\cos^2 1}x - \frac{1}{\cos^2 1} + \tan 1$ c) $y = -\frac{3}{8}(\ln 2)x + \frac{3}{8} \ln 2 + 1/8$.

11. List two ways a function can be continuous but not differentiable at the same point.

The function could have a corner or a vertical tangent.