

1. Find  $dy/dx$  for the following:  $x^2 - xy + y^3 = 8$ ,  $\sqrt{x+y} + \sqrt{xy} = 8$ ,  $x\sqrt{1+y} + y\sqrt{1+2x} = 2x$   
 Explain how to find where the tangents are horizontal and vertical (these may require solving a difficult equation; you will not be required to solve the difficult ones on this test, but possibly on the final)?

2. Find the tangent line to  $y^2 = x^3(2-x)$  at  $(1,1)$ ,  $2(x^2 + y^2)^2 = 20(x^2 + y^2)$  at  $(3,1)$

3. Find the following limits:

$$\lim_{x \rightarrow 0} \frac{1 - \cos 2x}{x^2}$$

$$\lim_{x \rightarrow \infty} \frac{\ln x}{x}$$

$$\lim_{x \rightarrow 0^+} \frac{x}{\ln x}$$

$$\lim_{x \rightarrow \infty} \frac{\ln(\ln x)}{\sqrt{x}}$$

$$\lim_{x \rightarrow \infty} x^2 e^{-x}$$

$$\lim_{x \rightarrow 0} \frac{x \sin x}{x^2 + 1 - \cos x}$$

$$\lim_{x \rightarrow 0} \frac{\cos x}{x}$$

$$\lim_{x \rightarrow 0} \frac{\sin(ax)}{x}$$

$$\lim_{x \rightarrow 0} \frac{\sinh x}{x}$$

$$\lim_{t \rightarrow 0} \frac{\cosh t^2 - 1}{t^4}$$

4. Give the following lines in slope/intercept form:

$$x = 3 + 4t, \quad y = 2 + 8t$$

$$x = -2 + \frac{3}{4}t, \quad y = 2t$$

5. Give a parametrization of the circle of radius 4 centered at the origin which starts at  $(-4,0)$  and moves clockwise. Sketch graphs of  $x$  vs  $t$  and  $y$  vs  $t$  for a parametrization of a rectangle whose vertices are  $(0,0)$ ,  $(-3, 0)$ ,  $(-3, -1)$ ,  $(0, -1)$  which starts at  $(0,0)$  and moves counterclockwise.

6. Chapter 4 Check your understanding: 1,2,3,5,6,7,8,9,10,11,16,14,18

7. Chapter 4 Review: 1,2,3,5,6,15,20, 23, 27,28,29,33, 37a

8. a. Find two numbers whose sum is 100 and whose product is a maximum

b. Find the points on the hyperbola  $y^2 - x^2 = 4$  that are closest to the point  $(2,0)$ .

c. If 1200  $\text{cm}^2$  of material is available to make a box with a square base and open top, find the largest possible volume.

d. A farmer with 750 ft of fencing wants to enclose a rectangular area and then divide it into 4 pens with fencing parallel to one side of the rectangle. What is the largest possible total area of the 4 pens.

9. Find the best possible bounds for the following:  $e^{-x^2}$  on  $[-1, 1]$ ,  $\sin 4x$  on  $[-\pi/2, \pi/6]$ ,  $Ae^{-x} + Be^x$  for  $A > 0$  and  $B > 0$ .