

Math 250a (Kennedy) - Quiz 11 - Fall '07

1. Show how to reduce $y' + \frac{y}{x} + xy^2 = 0$ to a linear differential equation. You do not need to solve the linear equation.

$$n = 2 \quad 1 - n = -1$$

so let $u = y^{-1}$

$$u' = -y^{-2} y' = -y^{-2} \left(-\frac{y}{x} - xy^2 \right)$$

$$= \frac{1}{xy} + x$$

$$= \frac{1}{x} u + x$$

so $u' = \frac{1}{x} u + x$ OR $u' - \frac{1}{x} u = x$

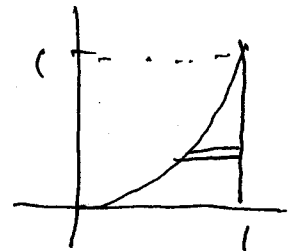
2. The region bounded by $y = x^2$, the x -axis, and the vertical line $x = 1$ is rotated about the horizontal line $y = 1$. Find the resulting volume.

slice \perp to y -axis

$$\text{slice vol} = (1-x) 2\pi (1-y) \Delta y$$

$$\text{vol} = \int_0^1 (1-x) 2\pi (1-y) dy$$

$$= \int_0^1 (1-\sqrt{y}) 2\pi (1-y) dy = \dots = \boxed{\frac{7\pi}{15}}$$



OR

slice \perp to x -axis

$$\text{slice vol} = \pi [1^2 - (1-x^2)^2] \Delta x$$

$$\text{vol} = \int_0^1 \pi [1^2 - (1-x^2)^2] dx$$

$$= \dots = \boxed{\frac{7\pi}{15}}$$

