

Formulae:

Distance between 2 points:

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2} : \text{this is the Pythagorean Theorem.}$$

$$\text{Midpoint: } m = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$\text{Slope: } \frac{(y_1 - y_2)}{(x_1 - x_2)} = m$$

$$\text{Perpendicular lines: } m_1 = -\frac{1}{m_2}$$

$$\text{Parallel lines: } m_1 = m_2$$

$$\text{Vertical line: } x = \text{constant}$$

$$\text{Horizontal line: } y = \text{constant}$$

$$\text{Inverse functions: } (f(f^{-1}(x))) = x$$

Exponential:

$$e^x = b \text{ implies}$$

$$\ln(b) = x$$

Limit definition of derivative:

$$\lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x} = f'(x)$$

$$\text{Average rate of change: } \frac{f(b) - f(a)}{b - a}$$

For related rates or optimization problems:

$$\text{Pythagorean theorem: } a^2 + b^2 = c^2$$

$$\text{Circle: } A = \pi r^2, P = 2\pi r$$

$$\text{Rectangle: } A = wl, P = 2l + 2w$$

$$\text{Box (closed top): } SA = 2wl + 2wh + 2hl, V = wlh$$

$$\text{Cylinder: } SA = 2\pi r^2 + 2\pi rh, V = \pi r^2 h$$

Differentiation rules:

$$\frac{d}{dx}(f(x)^n) = n(f(x))^{n-1} f'(x)$$

$$\frac{d}{dx}(e^{f(x)}) = e^{f(x)} f'(x)$$

$$\frac{d}{dx}(\ln(f(x))) = \frac{1}{f(x)} f'(x)$$

$$\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{f'g - g'f}{g^2}$$

$$\frac{d}{dx}(f(x)g(x)) = f'g + g'f$$

$$\frac{d}{dx}(\text{constant}) = 0$$

Integration by parts:

$$\int f g' dx = fg - \int f' g dx$$

(but I will give this one to you on the final)