

## Math 322 Section 3 Written Homework 2

1) Consider the matrix

$$A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}.$$

Compute its eigenvalues and corresponding eigenvectors (note: you may need to use complex numbers).

2) Consider the following matrix:

$$B = \begin{pmatrix} 11 & -5 & 5 \\ 7 & -1 & 7 \\ -1 & 1 & 5 \end{pmatrix}$$

- A) Compute the eigenvalues of the matrix.
- B) Compute the corresponding eigenvectors.
- C) Show that the eigenvectors span all of  $\mathbb{R}^3$  (Note:  $\mathbb{R}^3$  denotes all vectors with three real number components).

3) Consider the following matrix:

$$C = \begin{pmatrix} 2 & 1 & 0 \\ -1 & 0 & 1 \\ 1 & 3 & 1 \end{pmatrix}$$

- A) Compute the eigenvalues of the matrix.
- B) Compute the corresponding eigenvectors.
- C) Show that the eigenvectors do not span all of  $\mathbb{R}^3$  (Note:  $\mathbb{R}^3$  denotes all vectors with three real number components).

4) Consider the problem  $Mx = 0$  where  $M$  is a square matrix and  $x$  is a vector of unknowns. Give three different conditions on  $M$  that each ensure that  $M$  has only one solution. What is that solution?