

## Brief table of Fourier transforms

We define the transform as

$$F(k) = \int_{-\infty}^{\infty} e^{-ikx} f(x) dx$$

(note that Haberman's text adds a factor of  $1/2\pi$  in the transform and conversely deletes a factor of  $1/2\pi$  in the inverse transform).

| Description           | Function             | Transform               |
|-----------------------|----------------------|-------------------------|
| Delta function in $x$ | $\delta(x)$          | 1                       |
| Delta function in $k$ | 1                    | $2\pi\delta(k)$         |
| Exponential in $x$    | $e^{-a x }$          | $\frac{2a}{a^2+k^2}$    |
| Exponential in $k$    | $\frac{2a}{a^2+x^2}$ | $2\pi e^{-a k }$        |
| Gaussian              | $e^{-x^2/2}$         | $\sqrt{2\pi}e^{-k^2/2}$ |
| Derivative in $x$     | $f'(x)$              | $ikF(k)$                |
| Derivative in $k$     | $xf(x)$              | $iF'(k)$                |
| Translation in $x$    | $f(x-a)$             | $e^{-iak}F(k)$          |
| Translation in $k$    | $e^{iax}f(x)$        | $F(k-a)$                |
| Dilation in $x$       | $f(ax)$              | $F(k/a)/a$              |
| Convolution           | $f(x)*g(x)$          | $F(k)G(k)$              |