

1. Give values so that the table represents an invertible function

|        |      |            |             |      |      |
|--------|------|------------|-------------|------|------|
| $m$    | 1    | 2          | 3           | 4    | 5    |
| $f(m)$ | 0.09 | <u>3.2</u> | <u>5.91</u> | 7.80 | 9.40 |

For example - The values must be increasing

2. For what values of  $A$  and  $K$  will  $S(t) = At^3 - K$  be a one-to-one function?

$A$  and  $K$  can have any values except  $A=0$

3. Determine if the following functions are invertible.

- A.  $f(d)$  is the amount of sales tax on an item of clothing that sells for  $d$  dollars.

No The tax on \$10 is the same as the tax on \$9.99

- B.  $g(t)$  is the number of students waiting in line at the UA Catcard Office on the first day of classes as a function of time since the office opened that morning.

No The number of students increases and decreases during the day.

4. The life expectancy,  $L$ , of a child can be modeled by the function below. The variable  $y$  is the year of birth in relationship to 1980. For example,  $y=0$  corresponds to 1980.

$$L(y) = \frac{y + 96.94}{0.01y + 1.3}$$

- A. Give a practical interpretation of  $L(10)$ .

$$L(10) = \frac{10 + 96.94}{0.01(10) + 1.3} \approx 76.386$$

If a child is born in 1990, his or her life expectancy is about 76.4 years

- B. Give a practical interpretation of  $L^{-1}(78)$ .

This represents the number of years after 1980 a child is born who has a life expectancy of 78 years.

- C. Find the values of  $L(10)$  and  $L^{-1}(78)$ .

$$78 = \frac{y + 96.94}{0.01y + 1.3}$$

$$\begin{aligned} 78(0.01y + 1.3) &= y + 96.94 \\ 0.78y + 101.4 &= y + 96.94 \\ 4.46 &= 0.22y \\ y &= \frac{223}{11} = 20.27 \end{aligned}$$

So, if life expectancy is 78 years, the child was born in 2000.